

# Aerodynamic Design Optimization of a Transonic Strut-Braced-Wing Regional Aircraft

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Timothy Chau and David W. Zingg

University of Toronto Institute for Aerospace Studies



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# Introduction

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# Motivation

- Growing concerns surrounding the environmental sustainability of commercial aviation has motivated the need for greener aircraft
  - IATA: Reduce fuel burn and CO<sub>2</sub> emissions by 50% by 2050, relative to 2005 levels
- Step changes in environmental impact will require major advances from various areas:
  - Advanced aerodynamic technologies
  - Advanced structures and materials
  - Advanced propulsion technologies
  - Alternative fuels
- One major contribution is anticipated to come from **unconventional aircraft configurations** that have the potential to provide major savings in fuel burn, relative to the conventional tube and wing design



# Unconventional Aircraft Configurations





# Strut- and Truss-Braced Wings

## Advantages

- **Significantly lower induced drag** due to larger wing span
- **Higher structural efficiency** due to truss topology
  - Supports higher wing bending loads
  - Enables thinner wings
  - Lowers structural weight



## Aerodynamic Design Challenges

- **Shock formation in truss region** due to flow acceleration in small enclosed space(s)
- **Flow interference + skin friction drag penalties** from strut members

Aerodynamic design challenges must be addressed at Mach 0.78-0.80 to obtain a **credible estimate for the fuel burn advantage** of the configuration.

# Aerodynamic Shape Optimization

- Aerodynamic shape optimization automates the design process through specified objective functions, design variables and constraints, eliminating the need for extensive *a priori* design experience
- Aerodynamic shape optimization based on the Reynolds-averaged Navier-Stokes (RANS) equations:
  - Captures shock formation, boundary-layer separation, and nonlinear interference effects
  - Accurately captures and enables tradeoffs between induced drag, viscous drag, and wave drag

$$M = 0.78, Re = 20 \times 10^6$$

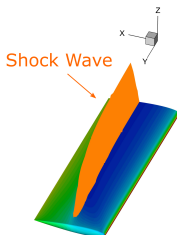
Initial

$$\alpha = 1.00^\circ$$

$$L/D = 8.7$$

$$C_L = 0.09$$

$$C_D = 0.0107$$



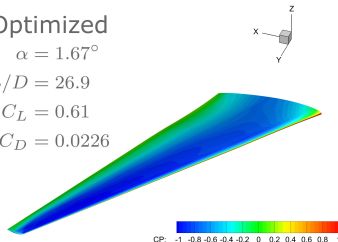
Optimized

$$\alpha = 1.67^\circ$$

$$L/D = 26.9$$

$$C_L = 0.61$$

$$C_D = 0.0226$$



# Questions to Address

1. Can we **mitigate shock wave formation** within the **wing-strut junction** at **high transonic Mach numbers** using high-fidelity aerodynamic shape optimization?
2. How do we design an optimal strut-braced-wing transport aircraft when accounting for **tradeoffs between induced drag, viscous drag, and wave drag**?
3. How much of a **fuel burn savings** can we expect over the conventional tube-and-wing for the **strut-braced-wing configuration** in the **regional jet class** with **current technology levels**?

This work will attempt to answer these questions through the application of **Aerodynamic Shape Optimization** based on the Reynolds-averaged Navier-Stokes (RANS) equations.

A conventional tube-and-wing regional jet will also be optimized to serve as a performance baseline.

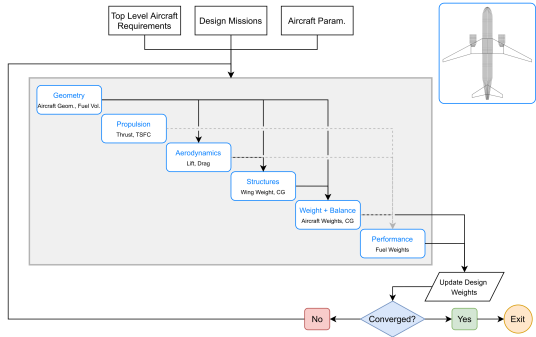


# Computational Design Tools

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# Faber: Conceptual Design Environment for Transport Aircraft

- Multidisciplinary design optimization (MDO) through low-order modeling
  - Aircraft system sizing
  - Top level aircraft requirements
  - Mission performance
- For unconventional wings:
  - Finite beam model for wing weight estimation
  - Global buckling detection
- Optimizes/sizes:
  - Wing planform
  - Tail planforms
  - Propulsion system
  - Operating conditions

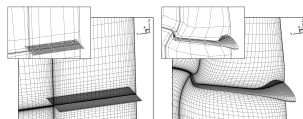


Sizing routine called by optimizer.

# Jetstream: High-Fidelity Aerodynamic Shape Optimization

## Mesh Parameterization and Deformation<sup>1</sup>, Geometry Control<sup>2</sup>

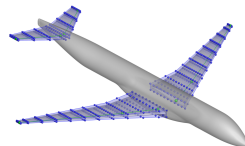
- B-spline volume parameterization
- Linear elasticity model for deforming B-spline volumes
- Axial and free-form deformation method



Mesh parameterization and deformation

## Structured Multiblock Flow Solver<sup>3</sup>

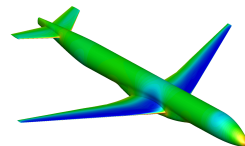
- Reynolds-averaged Navier-Stokes (RANS) equations fully-coupled with Spalart-Allmaras (SA) turbulence model; includes QCR2000
- Parallel implicit Newton-Krylov-Schur method



Geometry control system

## Optimization and Gradient Evaluation<sup>4</sup>

- SNOPT for gradient-based optimization
- Large-scale linear and nonlinear constrained problems
- Discrete adjoint method, analytical, complex step



Cp: -1 -0.8 -0.6 -0.4 -0.2 0 0.2 0.4 0.6 0.8 1

Optimized aerodynamic design

<sup>1</sup>Hicken and Zingg, *AIAA Journal*, 2010. doi: 10.2514/1.44033

<sup>2</sup>Gagnon, and Zingg, *AIAA Journal*, 2015. doi: 10.2514/1.J053575

<sup>3</sup>Osusky, M. and Zingg, *AIAA Journal*, 2013. doi: 10.2514/1.J052487

<sup>4</sup>Osusky, L. et al., *AIAA Journal*, 2015. doi: 10.2514/1.J053457

# Conceptual Design

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# Design Requirements: Missions and Sizing

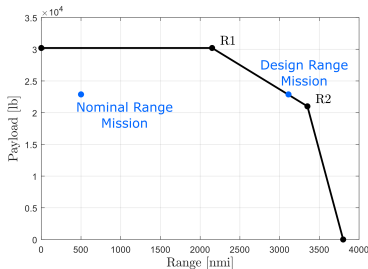
## Reference aircraft: Embraer E190-E2

- Maximum payload = 30,200 lb
- Design payload = 104 passengers
- Design range = 3,100 nmi
- Nominal range = 500 nmi
- Mach 0.78
- $W/S = 110.2 \text{ lb/ft}^2$ ,  $T/W = 0.336$
- Pratt & Whitney PW1919G engines



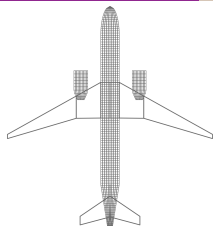
## Assume current technology levels for strut-braced wing

- Composite wing structures
- No natural laminar flow wings
- No advanced flow control
- No new engine technology

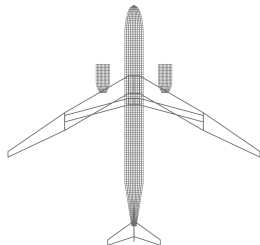




# Results: Conceptual-Level MDO



CTW100



SBW100

Parameter	CTW100	SBW100	$\Delta$
<i>Geometry</i>			
Mean aerodynamic chord [ft]	12.82	8.35	-
Span [ft]	110.6	136.0	-
Aspect ratio [-]	10.84	17.32	+59.8%
Wing wetted area [ft <sup>2</sup> ]	1,914	2,603	+36.0%
Reference area [ft <sup>2</sup> ]	1,129	1,068	-
<i>Weights</i>			
MTOW [lb]	124,290	117,710	-5.3%
MZFW [lb]	102,870	98,790	-
OEW [lb]	72,670	68,590	-5.6%
MFW [lb]	30,130	26,200	-13.0%
Maximum payload	30,200	30,200	-
Design payload (104 PAX)	22,880	22,880	-
<i>Propulsion</i>			
Maximum TO thrust (per engine) [lb]	20,860	19,780	-
Cruise TSFC [lb/lb/hr]	0.5872	0.5900	+0.5%
<i>Aerodynamics</i>			
Mach number [-]	0.78	0.78	-
Initial cruise altitude [ft]	37,000	44,670	-
Reynolds number [million]	22.04	9.92	-
Cruise $L/D$ [-]	18.1	21.0	+16.0%
Cruise $C_L$ [-]	0.468	0.682	-
Cruise lift [lb]	101,720	97,000	-
Cruise drag [lb]	5,620	4,610	-
<i>Fuel</i>			
Block fuel [lb]	5,160	4,720	-8.5%

<sup>1</sup>All operating conditions and cruise parameters are in reference to the start of cruise for the 500 nmi mission

# High-Fidelity Aerodynamic Shape Optimization

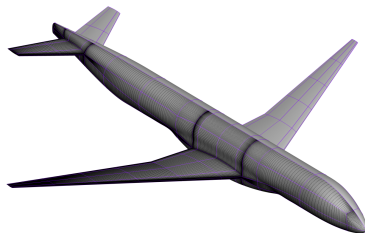
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# Geometry and Mesh

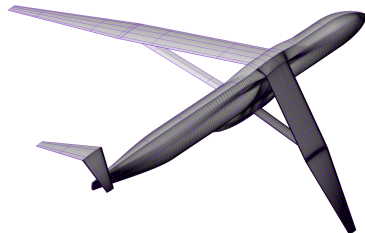
Grid	Num. of Nodes	Avg. Off-wall Spacing <sup>1</sup>	Average $y^+$
<i>Conventional Tube-and-Wing</i>			
L0	$14.41 \times 10^6$	$8.84 \times 10^{-7}$	0.53
L1	$27.56 \times 10^6$	$6.92 \times 10^{-7}$	0.41
L2	$54.85 \times 10^6$	$5.36 \times 10^{-7}$	0.31
<i>Strut-Braced Wing</i>			
L0	$26.51 \times 10^6$	$1.91 \times 10^{-6}$	0.57
L1	$50.50 \times 10^6$	$1.50 \times 10^{-6}$	0.43
L2	$99.54 \times 10^6$	$1.16 \times 10^{-6}$	0.33

<sup>1</sup>Off-wall spacings are in units of mean aerodynamic chord

- Based on Drag Prediction Workshop (DPW) gridding guidelines
- Optimize on *medium* mesh resolution, which is “representative of current engineering drag predictions”
- Richardson extrapolation performed post-opt. to estimate grid-converged  $C_L$ ,  $C_D$ , and  $L/D$



CTW100



SBW100

# Aerodynamic Shape Optimization Problem Definitions

## Conventional Tube-and-Wing

Objective Minimize cruise drag

Design Variables (281) Angle of attack (1)

Twist (16)

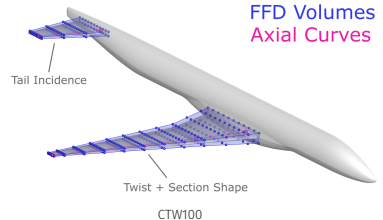
Section shape (264)

Nonlin. Constraints (13) Constant lift (1)

Zero pitching moment (1)

Minimum wing volume (1)

Minimum  $(t/c)_{\max}$  (10)



## Strut-Braced Wing

Objective Minimize cruise drag

Design Variables (946) Angle of attack (1)

Twist (43)

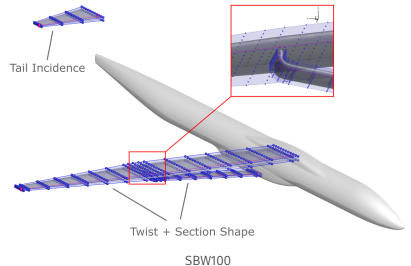
Section shape (902)

Nonlin. Constraints (33) Constant lift (1)

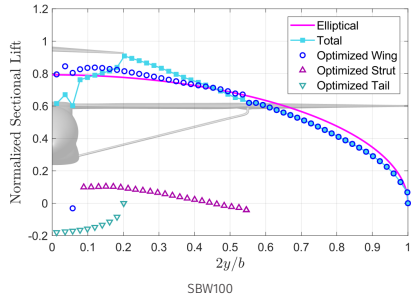
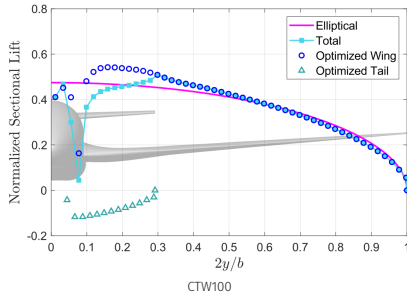
Zero pitching moment (1)

Minimum wing/strut volume (1)

Minimum  $(t/c)_{\max}$  (30)



# Results: Single-Point Optimized Spanwise Lift Distributions



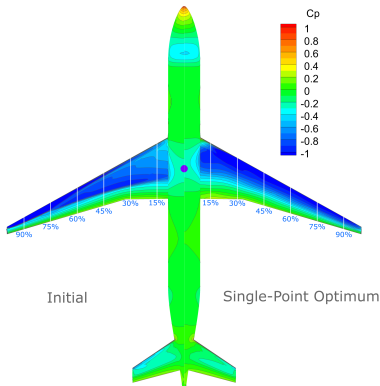
- Elliptical in form but shifted inboard due to trim constraint, and to avoid high sectional  $C_L$  over outboard portion of wing
- Negative lift over strut is introduced to alleviate adverse flow effects within wing-strut junction; compensated by more lift over inboard portion of wing
- Strut produces some lift near root

# Results: Single-Point Optimized CTW100

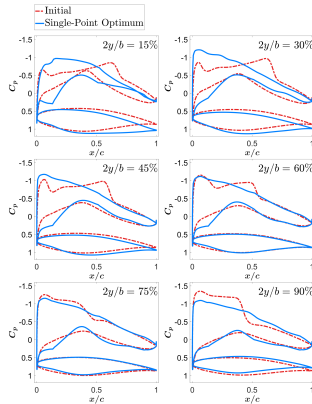
■ Lovely-Haimes
 Initial
Single-Point Optimum



Shock surfaces

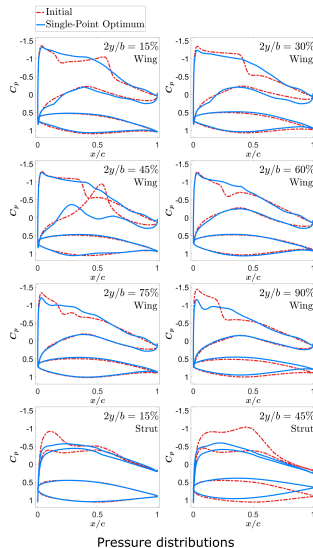
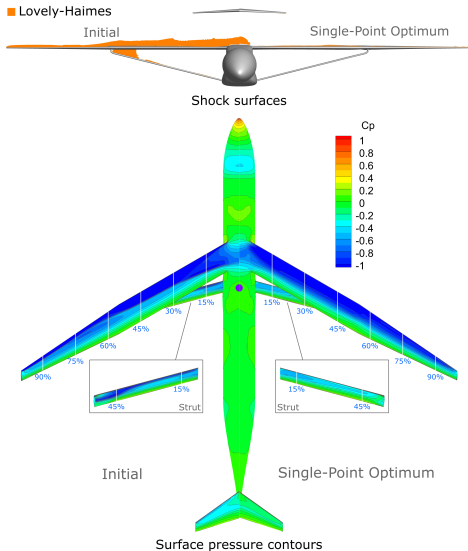


Surface pressure contours

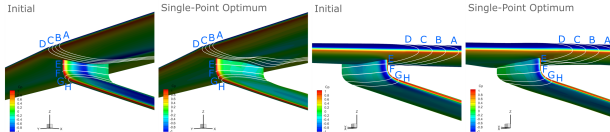


Pressure distributions

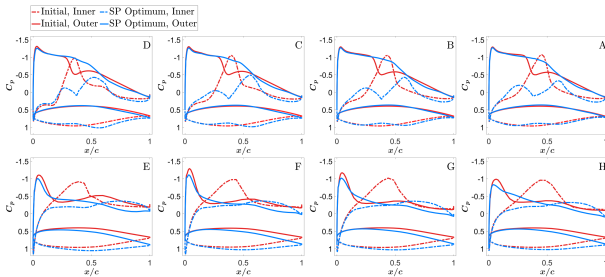
# Results: Single-Point Optimized SBW100



# Results: Junction Design and Performance



Inner (left) and outer (right) views of the wing-strut junction with surface pressure contours.

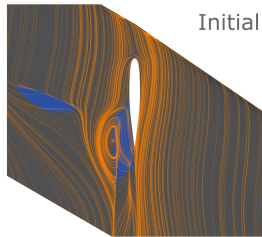
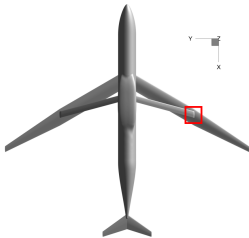


Airfoil profiles and pressure distributions over the wing and strut near the wing-strut junction.

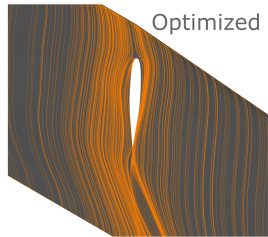
Novel airfoil shapes and an outwards force distribution over the strut helps alleviate the transonic channel effect and hence mitigates shock formation.



# Results: Junction Streamlines and Separation Surfaces

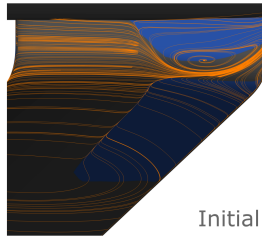
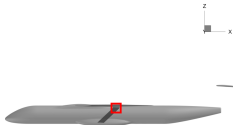


Initial

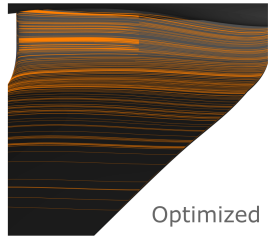


Optimized

A view of the lower wing surface.



Initial



Optimized

A view of the inner strut surface.

# Results: Single-Point Optimized Aircraft Performance

For **block fuel**, we reintroduce from the **low-order models**:

- Excrescence drag
- Drag for vertical tail, nacelles, and pylons
- Weight and propulsion
- Fuel from takeoff, climb, descent, and landing

Parameter	CTW100	SBW100	$\Delta$
Wing, Fuselage, Horizontal Tail (High Fidelity)			
Cruise $L/D$ [-]	22.33	24.46	+9.5%
Cruise $C_L$ [-]	0.468	0.682	+45.6%
Cruise $C_D$ [-]	0.0210	0.0279	+32.9%
Cruise lift [lb]	101,720	97,000	-4.6%
Cruise drag [lb]	4,555	3,966	-12.9%
Full Aircraft (Low + High Fidelity)			
Cruise $L/D$ [-]	18.96	21.40	+12.9%
Cruise $C_L$ [-]	0.468	0.682	+45.6%
Cruise $C_D$ [-]	0.0247	0.0318	+28.9%
Cruise lift [lb]	101,720	97,000	-4.6%
Cruise drag [lb]	5,365	4,532	-15.5%
Block fuel [lb]	5,028	4,643	-7.6%

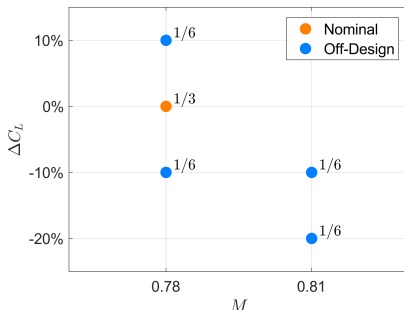
<sup>1</sup>Performance parameters are for the 500 nmi nominal mission.

# Multipoint Optimization Problem

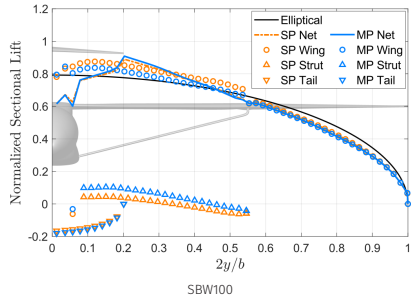
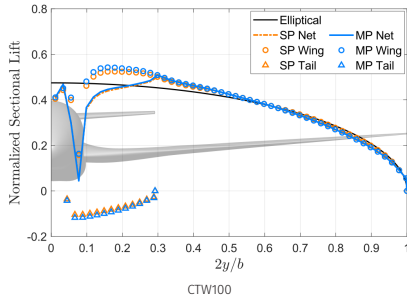
Can the low drag of the strut-braced-wing regional jet be maintained over a range of suitable cruise conditions? How does this impact block fuel performance?

$$\text{minimize } \mathcal{J} = \sum_{i=1}^N \mathcal{D}(M_i, C_{L_i}) C_D(M_i, C_{L_i})$$

- Includes  $\pm 10\% C_L$  conditions from the nominal design point
- Includes high speed design points at Mach 0.81
- Design weights selected to place  $2 \times$  priority on the nominal design point



# Results: Multipoint Optimized Spanwise Lift Distributions



- Negative lift on horizontal tail increased to compensate for higher inboard wing (and strut) loading
- Higher strut loading enables reduced wing loading to decrease wing  $C_L$

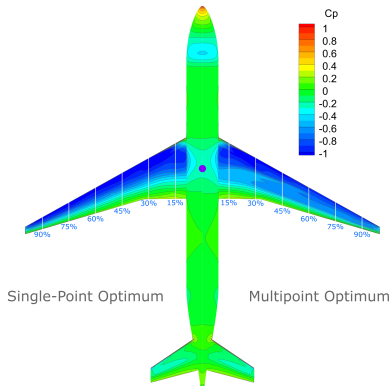
# Results: Multipoint Optimized CTW100

■ Lovely-Haimes

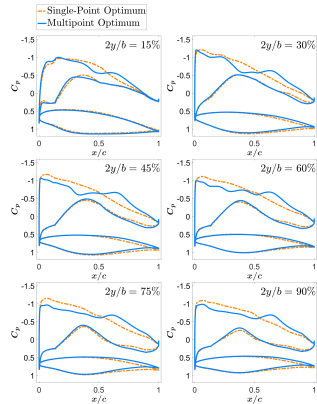
Single-Point Optimum      Multipoint Optimum



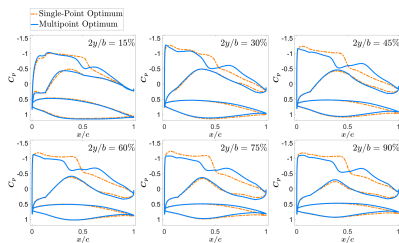
Shock surfaces



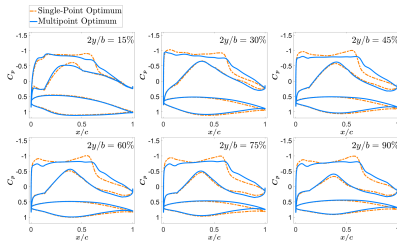
Surface pressure contours



# Results: CTW100 - Off-Design Performance



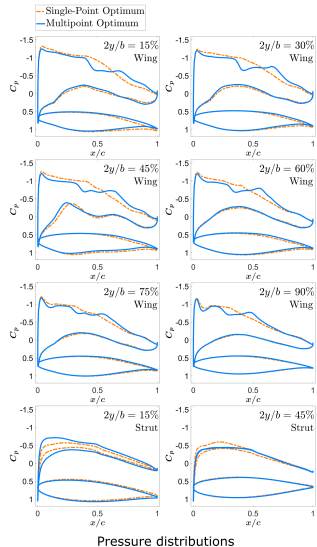
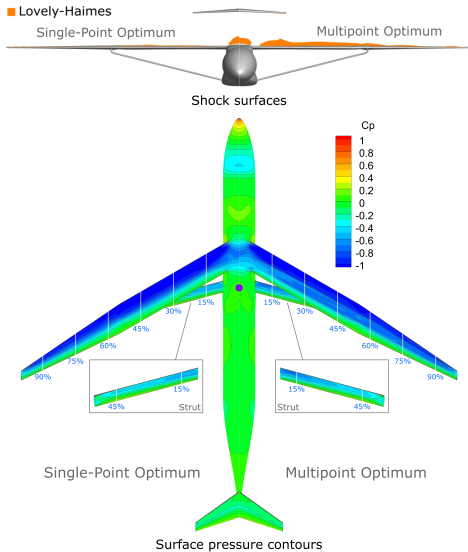
Design point 2:  $M = 0.78$  and  $C_L = 0.515$  (+10% nominal)



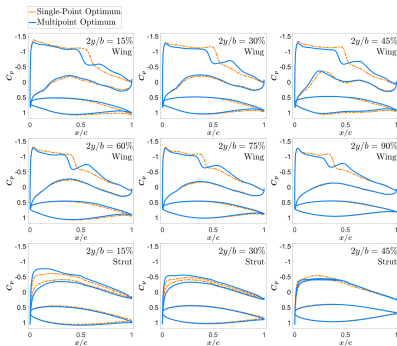
Design point 4:  $M = 0.81$  (+0.03 nominal) and  $C_L = 0.421$  (-10% nominal)

The optimizer adapts the wing design to improve off-design performance through a weakening of the shocks at those conditions.

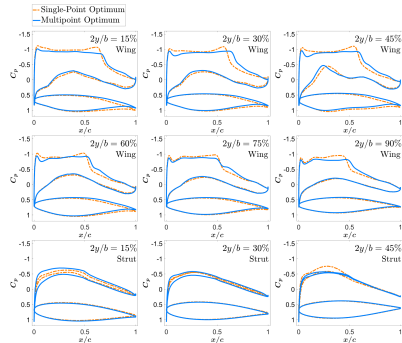
# Results: Multipoint Optimized SBW100



# Results: SBW100 - Off-Design Performance



Design point 2:  $M = 0.78$  and  $C_L = 0.750$  (+10% nominal)

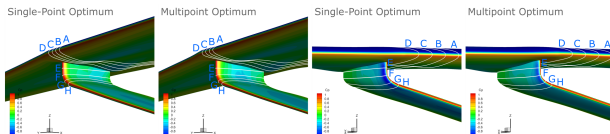


Design point 4:  $M = 0.81$  (+0.03 nominal) and  $C_L = 0.613$  (-10% nominal)

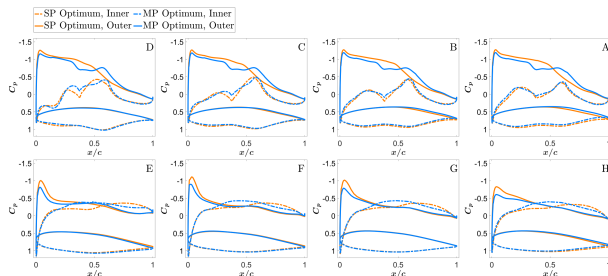
The optimizer adapts the wing design to improve off-design performance through a weakening of the shocks at those conditions. Strut lift also scales with the lift requirement.



# Results: Multipoint Optimum Junction Design and Performance



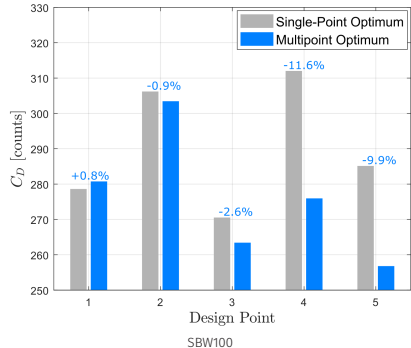
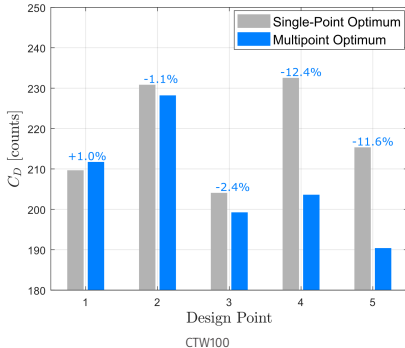
Inner (left) and outer (right) views of the wing-strut junction with surface pressure contours.



Airfoil profiles and pressure distributions over the wing and strut near the wing-strut junction.

The multipoint optimized junction design features are not very different from those of the single-point optimum.

# Results: Off-Design Performance



Multipoint optimization only compromises drag by 2 counts at the on-design point, while improving off-design performance by up to 29 and 36 counts for the CTW100 and SBW100, respectively.

# Results: Multipoint Optimized Aircraft Performance

Parameter	Single-Point Optimum			Multipoint Optimum		
	CTW100	SBW100	$\Delta$	CTW100	SBW100	$\Delta$
Wing, Fuselage, Horizontal Tail (High Fidelity)						
Cruise $L/D$ [-]	22.33	24.46	+9.5%	22.11	24.27	+9.8%
Cruise $C_L$ [-]	0.468	0.682	+45.6%	0.468	0.682	+45.6%
Cruise $C_D$ [-]	0.0210	0.0279	+32.9%	0.0212	0.0281	+32.6%
Cruise lift [lb]	101,720	97,000	-4.6%	101,720	97,000	-4.6%
Cruise drag [lb]	4,555	3,966	-12.9%	4,716	4,093	-13.2%
Full Aircraft (Low + High Fidelity)						
Cruise $L/D$ [-]	18.96	21.40	+12.9%	18.80	21.26	+13.1%
Cruise $C_L$ [-]	0.468	0.682	+45.6%	0.468	0.682	+45.6%
Cruise $C_D$ [-]	0.0247	0.0318	+28.9%	0.0249	0.0321	+28.7%
Cruise lift [lb]	101,720	97,000	-4.6%	101,720	97,000	-4.6%
Cruise drag [lb]	5,365	4,532	-15.5%	5,411	4,563	-15.7%
Block fuel [lb]	5,028	4,643	-7.6%	5,050	4,657	-7.8%

<sup>1</sup>Performance parameters are for the 500 nmi nominal mission.



## Conclusions and Future Work

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# Conclusions and Future Work

## Conclusions

- Demonstrated the feasibility of designing a low-drag transonic strut-braced wing through *single-point* and *multipoint* aerodynamic shape optimization based on the RANS equations
- Mitigated shock formation and boundary-layer separation from the wing-strut junction at Mach 0.78
- With current technology levels, [the optimized strut-braced-wing regional jet offers a 7.8% reduction in block fuel over a 500 nmi mission](#) compared to a similarly-optimized E190-E2-like conventional tube-and-wing regional jet

## Future Work

- Investigate the relative [fuel burn savings of a strut-braced-wing single-aisle transport aircraft](#)





Financial support and compute resources provided by:



UNIVERSITY OF  
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# CTW100: Conceptual Sizing Problem Definition

## Objective (1):

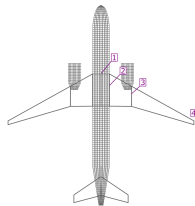
minimize Block fuel burn

## Design variables (4):

w.r.t. Wing thickness-to-chord ratio (4)

## Nonlinear constraints (1):

s.t. Min. fuel volume (1)



Thickness-to-chord ratio design variable locations

# SBW100: Conceptual Sizing Problem Definition

## Objective (1):

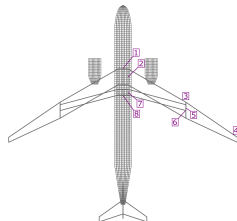
minimize    Block fuel burn

## Design variables (29):

w.r.t.    Wing/strut chord (8)  
          Wing/strut thick-to-chord ratio (8)  
          Horizontal tail chord (2)  
          Horizontal tail span (1)  
          Horizontal tail x-location (1)  
          Horizontal tail z-location (1)  
          Vertical tail chord (2)  
          Vertical tail span (1)  
          Vertical tail x-location (1)  
          Max. takeoff thrust (1)  
          Initial cruise altitude (3)

## Nonlinear constraints (27):

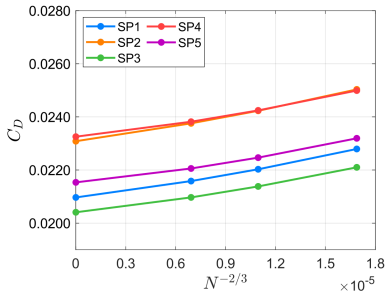
s.t.    Min. fuel volume (1)  
          Max. wing loading (1)  
          Min. thrust-to-weight ratio (1)  
          Min. top-of-climb thrust (3)  
          Min. static margin (2)  
          Min. buckling margin (5)  
          Min. buffet margin (12)  
          Min. horiz. tail volume ratio (1)  
          Min. vert. tail volume ratio (1)



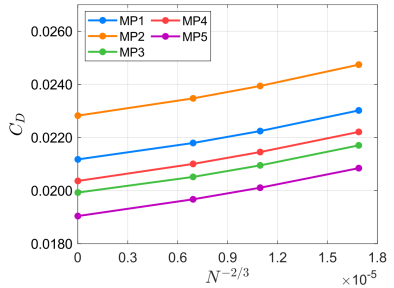
Thickness-to-chord ratio and Chord design variable locations



# CTW100: Grid Convergence Studies



Single-point optimum.



Multipoint optimum.

# SBW100: Grid Convergence Studies

